BOOK REVIEWS

Mem. Amer. Math. Soc. 315, 1985]. Approximately one-third of the entries are q-continued fractions. Several of these are related to Ramanujan's only published continued fraction, the famous Rogers-Ramanujan continued fraction. However, most of the entries are new. For each entry the authors give a proof and/or provide a reference to a proof. They also discuss connections with other entries and with the works of others.

This is a scholarly work that requires careful reading and checking in order to be fully appreciated. However, there is nothing too technical to prevent it from being read by someone with little or no knowledge of continued fractions. Both the expert and non-expert will profit from studying its contents and will be sure to become Ramanujan fans. It is recommended reading for anyone interested in special functions or approximations and expansions.

DAVID R. MASSON

Y. XU, Common Zeros of Polynomials in Several Variables and Higher Dimensional Quadrature, Pitman Research Notes in Mathematics Series 312, Longman Scientific & Technical, Essex (U.K.), 1994.

This book collects some significant recent results in the theory of multidimensional quadrature formulas. Given a square positive functional $\mathscr{L}(f)$ on the space of the multivariate polynomials, a quadrature formula is an approximation of this functional of the form $\sum_{k=1}^{N} \lambda_k f(\mathbf{x}_k)$ that is exact for all polynomials f up to a certain degree. The nodes \mathbf{x}_k are restricted to be real and the weights λ_k to be positive.

As in the one-dimensional case, the theory of quadrature formulas is based on the theory of orthogonal polynomials. The author uses a compact vector notation for the orthogonal polynomials and in a preliminary chapter he reviews their theory. The nodes of the quadrature formula are described as the common zeros of a set of quasi-orthogonal multivariate polynomials, which depend on matrices of parameters. Rather than relying on algebraic geometry for studying the common zeros of these polynomials, the author constructs properly tailored truncated block Jacobi matrices so that the common zeros of the polynomials are joint eigenvalues of these matrices. This leads to a characterization of the sets of quasi-orthogonal polynomials that generate interpolatory quadrature formulas with real nodes and positive weights. This characterization takes the form of nonlinear matrix equations in the parameters of these sets. Theorems 4.1.4 and 7.1.4 are, however, not properly formulated so that the reader may wrongly think that it is a characterization of the sets of polynomials whose common zeros are all real. The approach of the author is general; it deals with quadrature formulas of odd degree as well as of even degree. The relation with Möller's lower bound is explored in a separate chapter. Another chapter illustrates the theory with examples for which the nonlinear matrix equations can be solved.

The book is a research paper recommended to persons interested in the theoretical aspects of multidimensional quadrature and in multivariate orthogonal polynomials. It is selfcontained and assumes no specific knowledge.

PIERRE VERLINDEN

K. KITAHARA, Spaces of Approximating Functions with Haar-like Conditions, Lecture Notes in Mathematics 1576, Springer-Verlag, 1994, x + 110 pp.

The book contains five chapters and two appendices, with each chapter containing a problems section. A considerable portion of the book is based on the author's own work, some of which has not yet appeared elsewhere.

Chapter 1 introduces the Haar-like conditions mentioned in the title, and the definitions of $H_{\mathcal{F}}$, $T_{\mathcal{F}}$, and $WT_{\mathcal{F}}$ -systems, where \mathcal{F} is a set of *n*-tuples of linear functionals. Haar,